

Lattice Activities

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Outline

I. Introduction: Lattice @BNL...very special for over ¼ century!

II. Hunting New Physics with the lattice

III. Summary & Outlook

Introduction

- Lattice studies/simulation very special part of BNL-activities for over quarter of a century!**Michael Creutz's** name is essentially synonymous with lattice simulation...pioneering work now blossomed into a significant component of High Energy & Nuclear Physics communities.
- **'05 heralds significant new developments @BNL:**
 - a) **QCDOC 10 TfRBC machine**
 - b) arrival of **Frithjof Karsch**....adds important new directions in the arena of finite temperature simulations.
 - c) **QCDOC 10 TfDOE machine**
 - d) **RBC joins forces with UKQCD**

II. Hunting New Physics with the lattice

- 1) Recapitulate: why lattice is needed
- 2) Lattice helps reach a milestone in Particle Physics
- 3) Precise determination of the unitarity triangle... THE HOLY GRAIL
- 4) Exact chiral symmetry on the lattice
- 5) 20 years of B_K
- 6) RBC-Menu'05
- 7) B versus K-UT

Why Lattice is Needed

Due to the non-perturbative nature of low energy QCD, many experimental results, often attained at enormous cost cannot be used effectively to test the Standard Model unless accurate values of hadronic matrix elements are known; lattice is the only reliable tool for such calculations

$|\varepsilon_K|$ (BNL '64; Christenson et al), provides a **CLASSIC EXAMPLE**.

$$|\varepsilon_K| = \hat{B}_K C_K \lambda^6 A^2 \bar{\eta} \{ \eta_1 S(x_c) + \eta_2 S(x_t) [A^2 \lambda^4 (1 - \bar{\rho})] + \eta_3 S(x_c, x_t) \} \quad C_K = \frac{G_F^2 f_K^2 m_K m_W^2}{6\sqrt{2}\pi^2 \Delta m_K}$$

The experimentally known value $|\varepsilon_K| = 2.27 \times 10^{-3}$ can be used to extract information on the poorly known SM parameters $\bar{\rho}$ and $\bar{\eta}$, once the non-perturbative quantity, B_K becomes known, as everything else on the RHS is known quite well.

$$V_{\text{CKM}} =$$

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}. \quad (12.5)$$

CKM-matrix in the Wolfenstein
Representation (PDG'04)

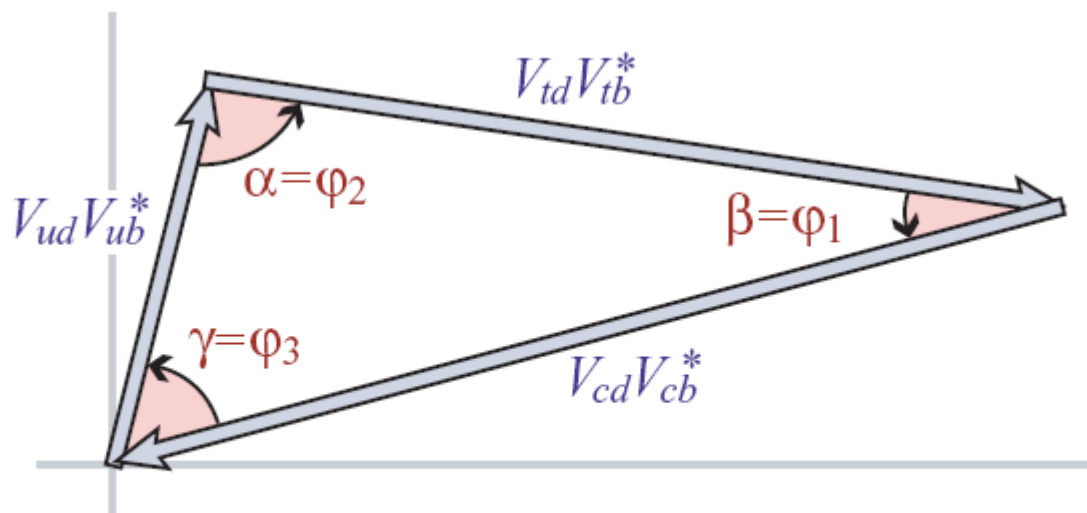
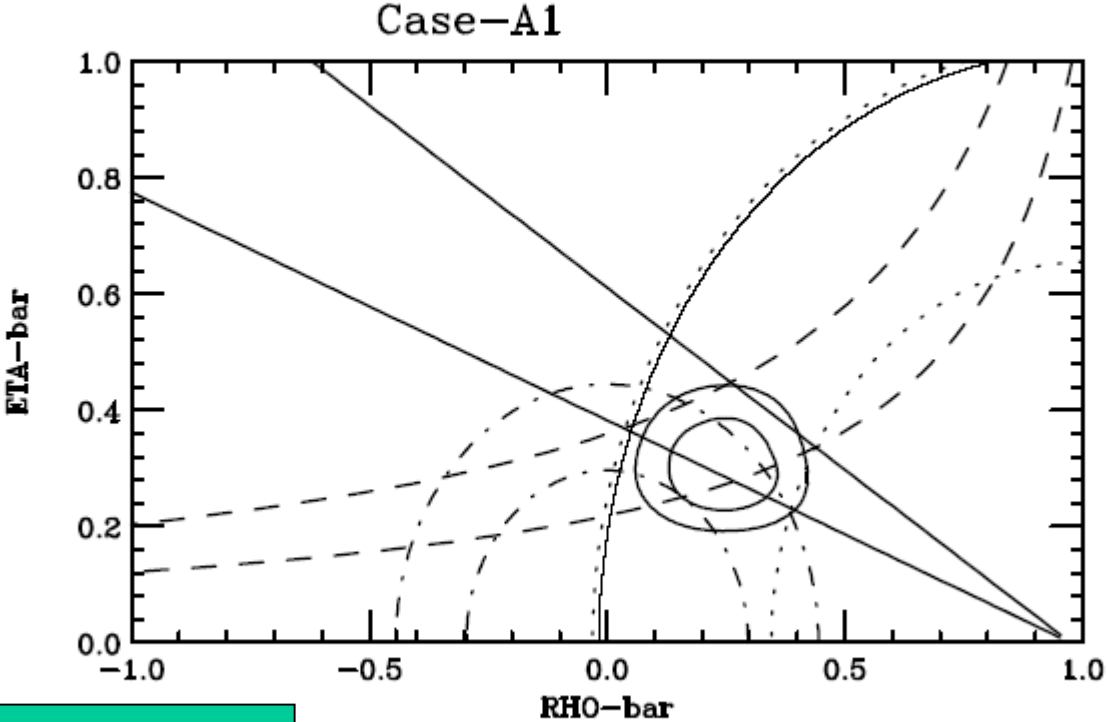


Figure 12.1: Graphical representation of the unitarity constraint $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$ as a triangle in the complex plane.

The unitarity triangle

1st Hints of confirmation Of CKM-CP violation

Atwood&A.S,
hep-ph/0103197



Most bands due
To theory errors

DOE-Review-4/27/05

SM prediction using existing experiments + lattice input

Table 1: Comparison of some fits.

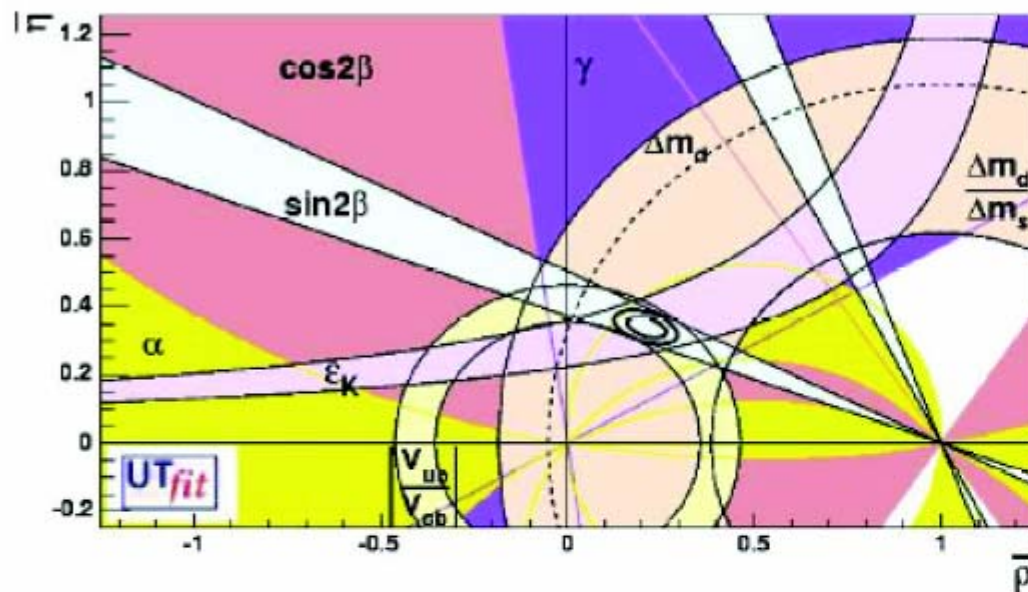
Input Quantity	Atwood & Soni ⁷	Ciuchini <i>et al</i> ⁸	Hocker <i>et al</i> ⁹
$R_{uc} \equiv V_{ub}/V_{cb} $	$.085 \pm .017$	$.089 \pm .009$	$.087 \pm .006 \pm .014$
$F_{B_d} \sqrt{\hat{B}_{B_d}}$ MeV	230 ± 50	$230 \pm 25 \pm 20$	$230 \pm 28 \pm 28$
ξ	$1.16 \pm .08$	$1.14 \pm .04 \pm .05$	$1.16 \pm .03 \pm .05$
\hat{B}_K	$.86 \pm 0.15$	$.87 \pm 0.06 \pm 0.13$	$.87 \pm .06 \pm .13$
Output Quantity			
$\sin 2\beta$	$.70 \pm .10$	$.695 \pm .065$	$.68 \pm .18$
$\sin 2\alpha$	$-.50 \pm .32$	$-.425 \pm .220$	
γ	$46.2^\circ \pm 9.1^\circ$	54.85 ± 6.0	56 ± 19
$\bar{\eta}$	$.30 \pm .05$	$.316 \pm .040$	$.34 \pm .12$
$\bar{\rho}$	$.25 \pm .07$	$.22 \pm .038$	$.22 \pm .14$
$ V_{td}/V_{ts} $	$.185 \pm .015$		$.19 \pm .04$
$\Delta m_{B_s} (ps^{-1})$	19.8 ± 3.5	$17.3^{+1.5}_{-0.7}$	24.6 ± 9.1
J_{CP}	$(2.55 \pm .35) \times 10^{-5}$		$(2.8 \pm .8) \times 10^{-5}$
$BR(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(0.67 \pm 0.10) \times 10^{-10}$		$(.74 \pm .23) \times 10^{-10}$
$BR(K_L \rightarrow \pi^0 \nu \bar{\nu})$	$(0.225 \pm 0.065) \times 10^{-10}$		$(.27 \pm .14) \times 10^{-10}$

Table 31: $S_{b \rightarrow c s}$ and $C_{b \rightarrow c s}$.

Experiment		$-\eta S_{b \rightarrow c s}$
BABAR	[192]	$0.722 \pm 0.040 \pm 0.023$
Belle	[58]	$0.728 \pm 0.056 \pm 0.023$
B factory average		0.725 ± 0.037
Confidence level		0.91
ALEPH	[193]	$0.84^{+0.82}_{-1.04} \pm 0.16$
OPAL	[194]	$3.2^{+1.8}_{-2.0} \pm 0.5$
CDF	[195]	$0.79^{+0.41}_{-0.44}$
Average		0.726 ± 0.037

Heavy-flavor
-averaging
Group, hep-ex
/0412073

Excellent
agreement ->
striking
confirmation of
the CKM-paradigm

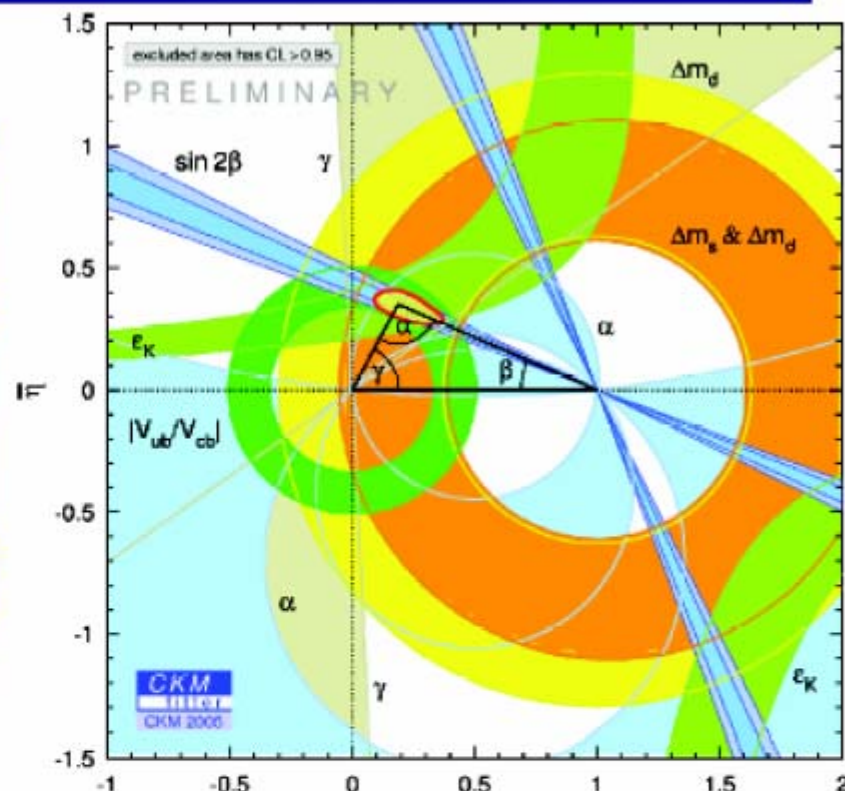


$$\bar{\rho} = 0.210 \pm 0.035$$

$$[0.139, 0.276] @ 95\% \text{ CL}$$

$$\bar{\eta} = 0.340 \pm 0.020$$

$$[0.300, 0.380] @ 95\% \text{ CL}$$



$$\bar{\rho} = 0.207^{+0.035}_{-0.045}$$

$$\bar{\eta} = 0.339^{+0.026}_{-0.021}$$

Lattice helps attain an important milestone in Particle Physics

- **I. B-factory results + lattice (despite severe limitations)**
-> CKM-paradigm of CP violation gives an excellent account simultaneously of CP violation in $K_L \rightarrow \pi\pi$ ($\epsilon_K \sim .001$) as well as $a_{CP}(B \rightarrow \psi K_S) \sim .73$ [SLAC/KEK] with $\eta \sim .30 \pm .05$!
- **II. Note w/o the lattice ~\$1 billion spent for the experimental #s would have been seriously shortchanged.**
- **III. This is an outgrowth of the calculation of weak matrix elements initiated in collaboration with Claude Bernard ~'83.**

20 years of B_K

C. Bernard, A. Soni / Weak matrix elements on the lattice

16

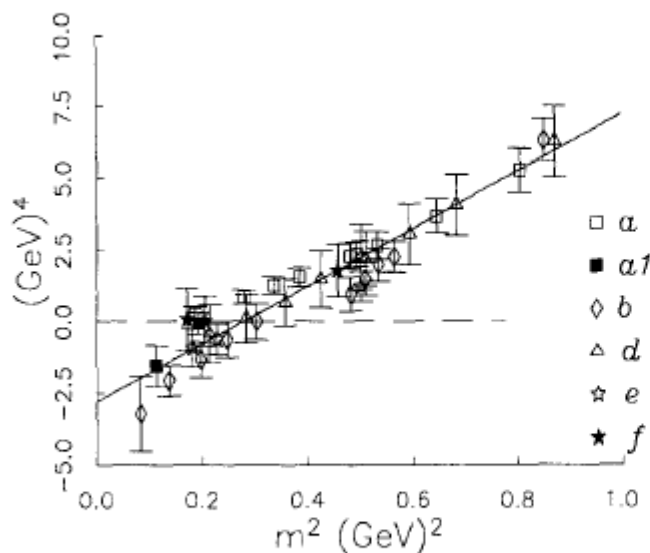


FIGURE 4
The amplitude $\langle \bar{K}^0 | (\Delta s = 2)_{LL} | K^0 \rangle \times 10^2$ vs. m^2 . The solid line is a naive (uncorrelated) fit to the data.

$\langle \bar{K}^0 | (\Delta s = 2)_{LL} | K^0 \rangle$ with Wilson fermions has been proposed in Ref. 32. One starts by writing the CPT form for the matrix elements of the continuum (physical) operator and for its Wilson lattice counterpart:

$$\begin{aligned} \langle \bar{K}^0 | (\Delta s = 2)_{LL} | K^0 \rangle^{\text{cont}} &= \gamma(p_K \cdot p_R) + \dots \\ \langle \bar{K}^0 | (\Delta s = 2)_{LL} | K^0 \rangle^{\text{latt}} &= \alpha + \beta m^2 + \gamma'(p_K \cdot p_R) + \dots, \end{aligned} \quad (8)$$

where the α and β terms in the lattice amplitude (and the change from γ to γ') are due to “bad” chirality operators such as O'_\pm which have not been correctly removed by perturbation theory. Note that for K, \bar{K} at rest, $p_K \cdot p_R = m^2$; while for the crossed amplitude $\langle \bar{K}^0 \bar{K}^0 | (\Delta s = 2)_{LL} | 0 \rangle$, $p_K \cdot p_R = -m^2$. Both the original $K^0 - \bar{K}^0$ amplitude and the crossed amplitude are then computed at rest on the lattice for various values of m , and the γ' term is extracted by a fit to the data. Finally, with the assumption $\gamma \simeq \gamma'$ (see below for a critique), the order m^2 term in the continuum ampli-

Bernard & A.S.
Lattice '88

Operator Mixing and B_K ...

- If chiral symmetry is broken, four other operators can mix (the four other possible gamma matrix structures)

$$\langle \bar{K}^0 | O_{VV+AA} | K^0 \rangle_{\text{latt}} \propto \langle \bar{K}^0 | O_{VV+AA} | K^0 \rangle_{\text{ren}} + \sum_{i \geq 2} c_i \langle \bar{K}^0 | O_{MIX,i} | K^0 \rangle_{\text{ren}}$$

These operators, of course, have a different chiral structure.

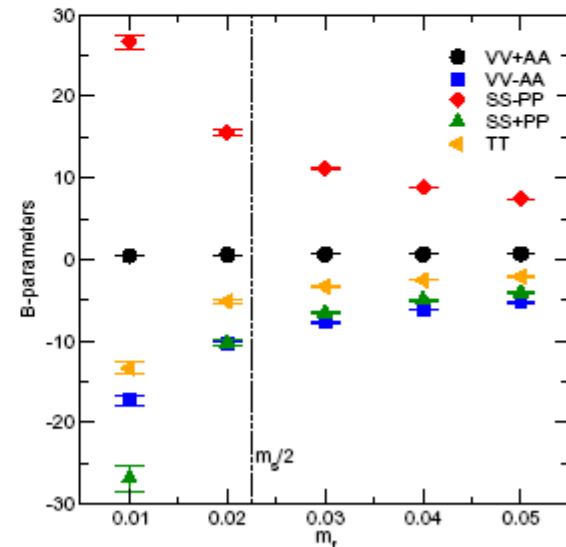
Mixing is hard to control using perturbation theory; First order chiral perturbation theory predicts that

$$\langle \bar{K}^0 | O_{VV+AA} | K^0 \rangle \propto M_k^2$$

and,

$$\langle \bar{K}^0 | O_{\text{THE REST}} | K^0 \rangle \propto \text{constant}$$

small enough mass, wrong chirality operators will **dominate**.

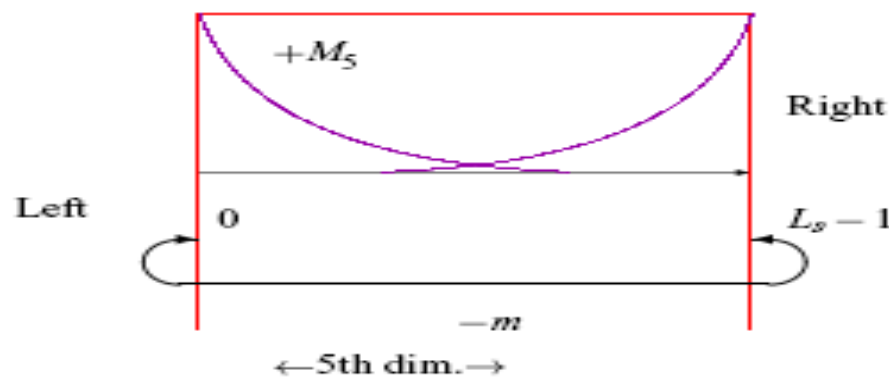


Lack of chiral symmetry
becomes a fine-tuning problem!

EXACT CHIRAL SYMMETRY ON THE LATTICE

Conventional fermions do not preserve chiral-flavor symmetry on the lattice (Nielsen - Ninomiya Theorem)
 $\Rightarrow \Delta S = 1, \Delta I = 1/2$ case mixing with lower dim. (power-divergent) operators & or mixing of 4-quark operators with wrong chirality ones makes lattice study of $K - \pi$ physics virtually impossible.

Domain Wall Fermions (Kaplan, Shamir, Narayanan and Neuberger)



Practical viability of DWF for QCD demonstrated (96-97) Tom Blum & A. S.

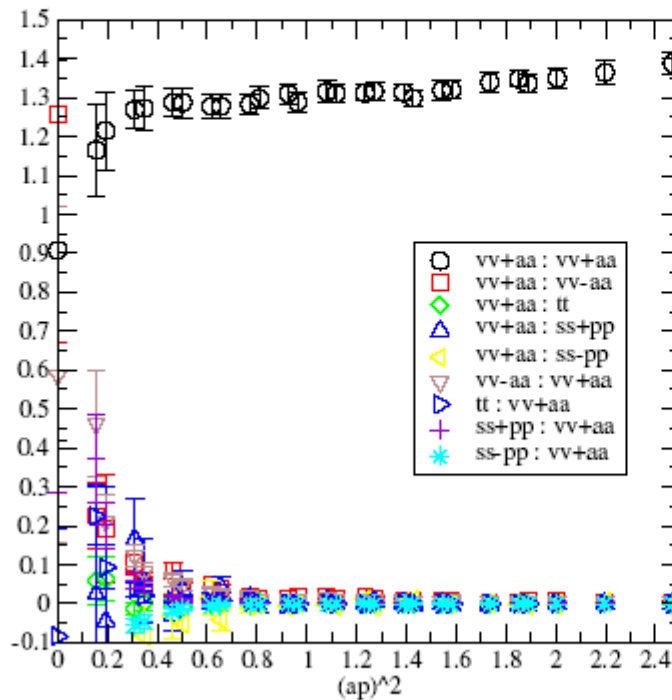
Chiral symmetry on the lattice, $a \neq 0$! Huge improvement

\Rightarrow Now widespread use at BNL and elsewhere

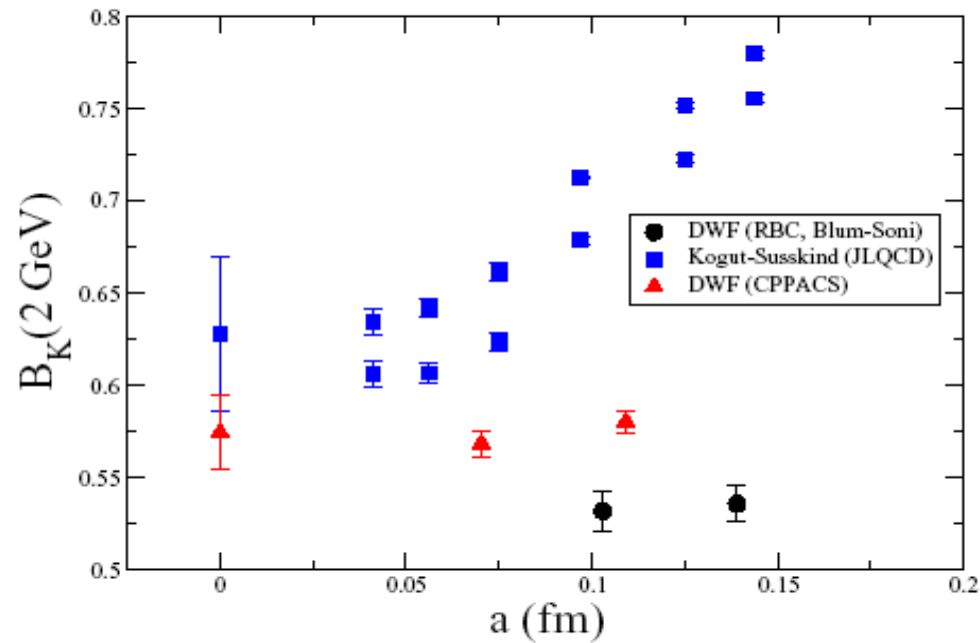
Z_{B_K} results

C Dawson@CKM'05

Elements of $(Z/Z_q)^{-1}$ (chiral limit)



- Mixing very small
- Combining Diagonal Z with perturbative matching calculation give the Z-factor in \overline{MS} , as required.



B_K with DWF's confronts staggered fermion results

Indications are that DWQ answer is 10-15% below the old (staggered) result \Rightarrow tends to correspondingly increase the CP violating phase $\bar{\eta}$ of the SM.

RBC, in prep.

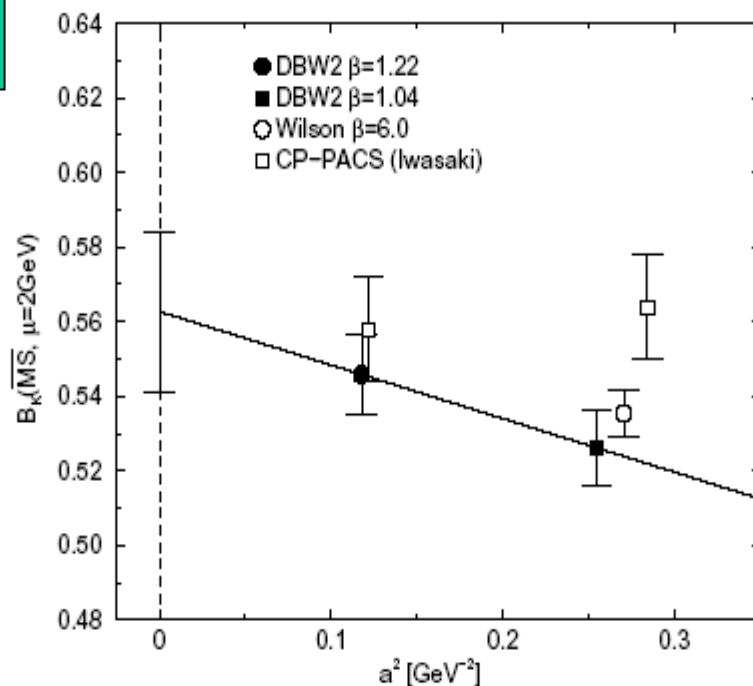


FIG. 29: Summary of our results of $B_K(\overline{\text{MS}} \text{ NDR}, \mu = 2 \text{ GeV})$ renormalized with $N_f = 0$ as a function of the lattice scale squared. While filled circles are our results, open symbols are quoted from previous works [20, 21].

theory. Within the quenched approximation, we extrapolate to zero lattice spacing and obtain $B_K^{\overline{\text{MS}} \text{ NDR}}(\mu = 2 \text{ GeV}) = 0.563(21)(-25)$, where the first error represents the statistical error and second one is the systematic error within our calculation. We also discuss other

Dynamical Domain Wall Fermions

3/2 years running on a 400GF partition of the 1TF QCDSP (the cell-phone supercomputer)

- 3 different dynamical masses
 - $0.5m_s \rightarrow m_s$
- two degenerate dynamical flavours
- $16^3 \times 32$; $((2\text{fm})^3 \times 4\text{fm})$
- 96 configurations/mass



Made possible by a lot of work on improving fermion algorithms and learning how the Domain Wall Fermion mechanism success depends on the Gauge Action used.

- Note: this is the “less quenched” approximation.
 - dynamical u and d; quenched s quark.
 - Stepping stone to 3 flavour dynamical DWF on QCDOC

C. Dawson

Results for B_K

RBC, hep-
lat/0411006

Fitting for valence and dynamical masses such that

$$0.02 \leq am_{\text{sea}}, am_{\text{val}} \leq 0.04$$

as for low valence masses the plateau quality is bad, and we wish to stay in the (relatively) low mass region to fit to NLO chiral perturbation theory

Fit	Bare Number	$\overline{MS}, 2\text{GeV}$
Degenerate	0.547(15)	0.509(18)
Non-degenerate	0.533(14)	0.495(18)

The difference between the degenerate and non-degenerate fits is within the quoted statistical error, but due to these errors being correlated it is actually statistically well resolved as a $2.8 \pm 0.03\%$ effect.

- In the quenched approximation studies using staggered fermions give [JLQCD, 1997]:

$$B_K(\overline{MS}, 2\text{GeV}) = 0.63(4)$$

Our quenched result with domain wall quarks is somewhat smaller: 0.563(21)(25)...this tends to increase η

Future



- This is a picture of the first **QCDOC** machine, taken a few days before it was shipped off to **Edinburgh** in **November**. The second machine (**RBRC**) is completely constructed and is currently being debugged. A third machine (shared by the US lattice community) will follow **very soon**. Each machine is capable of 10 TFlops.

RBC Menu'05

A **sample** of the physics we wish to study on these lattices:

Hadronic spectrum	Decay constants
Light quark masses	Static quark potential
Topological charge	→ Kaon B-parameter
→ $K \rightarrow \pi\pi$ decay	→ $K \rightarrow \pi l \nu$
Nucleon matrix elements	Excited nuclear states
Exotic hadrons, pentaquarks	Nucleon decay.
Neutron EDM	$g - 2$
Electromagnetic structure of hadrons	$U(1)_A$ problem
η' meson	Charm and bottom physics
Structure functions	

With a factor of 20 or more in computing power, clearly we would like to do lots of important physics. Unfortunately, HET has ZERO lattice post-doc (traditionally have had at least one)

B versus K Unitarity Triangle

Traditionally, experiment plus lattice matrix elements are used for ε_K , $B_d - \bar{B}_d$ mass difference (Δm_d) and semi-leptonic $b \rightarrow uev$ to constrain the unitarity triangle (UT)

\Rightarrow There ε_K provided crucial (and the only known) CP violation info. However, now that B-factories have seen large CP violation in $B \rightarrow \psi K_s$ and it is very “clean”, i.e. no hadronic uncertainties, one can replace input from ε_K in the above and construct UT purely from B-physics.

\Rightarrow In the future it would be important to construct another UT purely from K-physics using (greatly improved calculations) of hadronic matrix elements from the lattice, for ε_K , ε' along with improved experimental measurements of $K^+ \rightarrow \pi^+ + \nu + \bar{\nu}$ and possibly also $K_L \rightarrow \pi^0 + \nu + \bar{\nu}$.

\Rightarrow Comparison of the two UT's is likely to become a powerful new avenue to search for new physics.

Summary & Outlook

- **Lattice calculations of weak matrix elements along with B-factory results have led to a striking confirmation of the CKM-paradigm of CP violation.**
- **Since the KM-mechanism is dominant contributor to the observed CP violation in the K and B-systems, the effects of any new beyond the SM CP phase is likely to be small.**
- **This puts greater demands on precision from experiments as well as from theory for the discovery of new phenomena.**
- **For the lattice, the new hardware (QCDOC) would allow us to go beyond the quench approximation, a major source of error heretofore.**
- **To use the increased computing power effectively for physics applications of experimental interest, however, would require at least one possibly more lattice post-docs in HET; currently we have none.**